

McMaster University—DeGroote School of Business

Bus O711: Operations Analysis Under Uncertainty

Assignment #2 (Queueing Theory—Part 1)

Due Date: TBA

Late assignments will not be accepted!

Question	1	2	3	4	5	TOTAL
Mark	20	20	20	20	20	100

1. **Textbook¹ problem 17.2.2, p. 814 (Newell and Jeff)**
2. **Textbook problem 17.2.5, p. 814 (Midtown Bank)**
3. **Textbook problem 17.4.3, p. 815 (Machine repair)**
4. **Textbook problem 17.5.6 (except part f), p. 816 (Maintenance)**
5. **Pizza Industry**

You are doing an industry analysis of the Hamilton pizza industry. The rate (per year) at which pizza restaurants enter the industry is given by p , where $p =$ price of a pizza in \$. The price of a pizza is assumed to be $\max(0, 16 - .5j)$, where $j =$ number of pizza restaurants in Hamilton. During a given year the probability that a pizza restaurant fails is $1/(10 + p)$. Create a birth-death model of this situation.

- (a) In the steady state, estimate the average number of pizza restaurants in Hamilton.
- (b) What fraction of the time will there be more than 20 pizza restaurants in Hamilton?

HINT: Birth rate λ_j in this problem is thus $\lambda_j = p = \max(0, 16 - .5j)$ (state dependent) and the death rate is $\mu_j = j/(10 + p)$ (also state dependent).

¹F. S. Hillier and G. J. Lieberman, “Introduction to Operations Research,” 9th Edition, McGraw- Hill, 2009.